

Supplementary materials for Facies vectors: Disentangling environmental variability, diagenesis, and secular change in carbonate stratigraphies

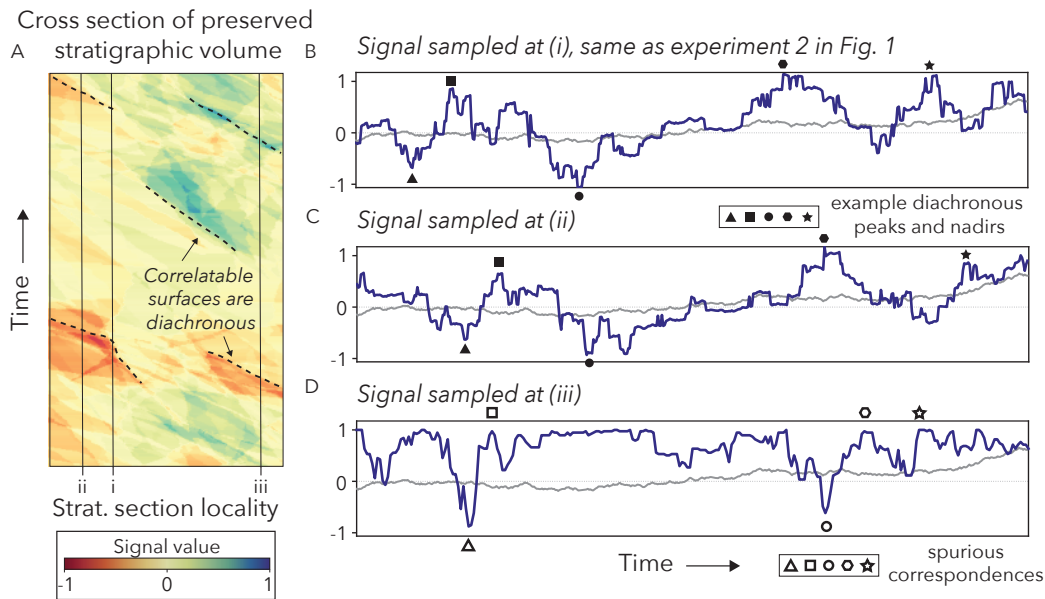
1 **Lateral variability and section correlations**

2 A common approach to potentially circumvent the contribution of sub-
3 environments is to measure parallel sections across a fossil platform to give
4 evidence that a signal stems from a broader trend. However, with migrating
5 lateral variability as a major source of stratigraphic excursions—manifest in
6 fossil assemblages, chemostratigraphic peaks and nadirs, or lithostratigraphic
7 observations—the data upon which correlations rely likely are diachronous
8 (Supplementary Figure 1). For instance, subaerial exposure markers ([Hill-
9 gaertner, 1998](#)), flooding surfaces ([Goldhammer et al., 1991](#)), and distinctive
10 stromatolite occurrences ([Hofmann, 1977](#)) are common markers for correlat-
11 ing sections. However, assuming that the entire platform was synchronously
12 exposed or covered by a uniform layer of stromatolites is, in itself, an inter-
13 pretation of large-scale secular change. A more neutral starting point based
14 upon current knowledge of modern platforms would be to say that prograd-
15 ing, exposed islands, and the unique conditions for distinctive stromatolites
16 existed on some portion of the platform throughout some of its history. As
17 part of the platform’s environmental mosaic, these conditions can to be sam-
18 pled by separate sections, but their occurrences most likely track migration.

19 This concept of surface diachroneity is not new, as this limitation often is
20 acknowledged in sequence stratigraphic frameworks of fluvial-deltaic environ-
21 ments (Wagoner et al., 1988) or depositional models for long-term cycles on
22 carbonate platforms driven by eustatic sea-level change Sarg (1988). Studies
23 of modern environments, however, now indicate that the assumption of di-
24 achroneity should apply even to chemical excursions (Geyman and Maloof,
25 2021) and short-term environmental transitions (Dyer et al., 2018, Geyman
26 et al., 2021)

27 These complications for correlation exist regardless of the relative dis-
28 tance separating sections. When parallel columns are nearby, separated by
29 less than the lengthscale of variability and track similar facies bodies (pos-
30 sibly the migration of the same stromatolite belt), their signals will have
31 high correspondence, but be offset in time (Figure 1A–C). Therefore, even if
32 a geologist can trace a bed over continuous outcrop for tens of kilometers,
33 correlations have a temporal precision limited by rates of facies migration or
34 platform subsidence (Drummond and Wilkinson, 1993, Burgess, 2001, Gey-
35 man et al., 2021). When sections are separated by more than the lengthscale
36 of variability, alignment no longer stems from the passing of the same depo-
37 sitional bodies and relies upon similar sequences of excursions (Figure 1D).
38 On carbonate platforms, similar cycles of depositional facies are expected
39 to be pervasive, as shallowing-up parasequences can result from autogenic
40 processes (Geyman et al., 2021, Burgess, 2001), which gives a mechanism
41 by which even distant stratigraphies can be correlated through signals that
42 neither are linked in cause, nor time. In either case of section alignment,
43 sub-environmental variability remains as the likely origin of the signal, and

44 so we still must answer a key question: What is the contribution of the local
 45 sub-environment that deposited each bed to the overall trend we see in the
 46 stratigraphy?



Supplementary Figure 1: Experiments from Figure 1 (main text) also illustrate how attempting to correlate parallel sections does not relieve ambiguity in assessing secular trends. (A) In a cross section of the preserved stratigraphic volume from experiment 2 in Figure 1 (main text), we see that surfaces representing extreme peaks and nadirs (and therefore the most recognizable for correlation) stem from lateral variability and are diachronous. (B,C) When we plot the signals from two parallel sections that are separated by less than the spatial lengthscale of variability, the most extreme peaks and nadirs that would be used for correlation are not part of the original signal and are offset in time. For this system, correlating parallel sections would not help disentangle local and secular changes, and would simply identify the migration of internal variabilities. (D) A signal that is separated from *i* and *ii* by more than the lengthscale of variability does not sample the same facies migrations. One could apply a null hypothesis that signals should correlate and assume differential accumulation rates that would dilate and contract this record to spuriously align sections, but correspondence would only relate to the passing of similar depositional conditions in a comparable sequence.

47 **Diagenesis**

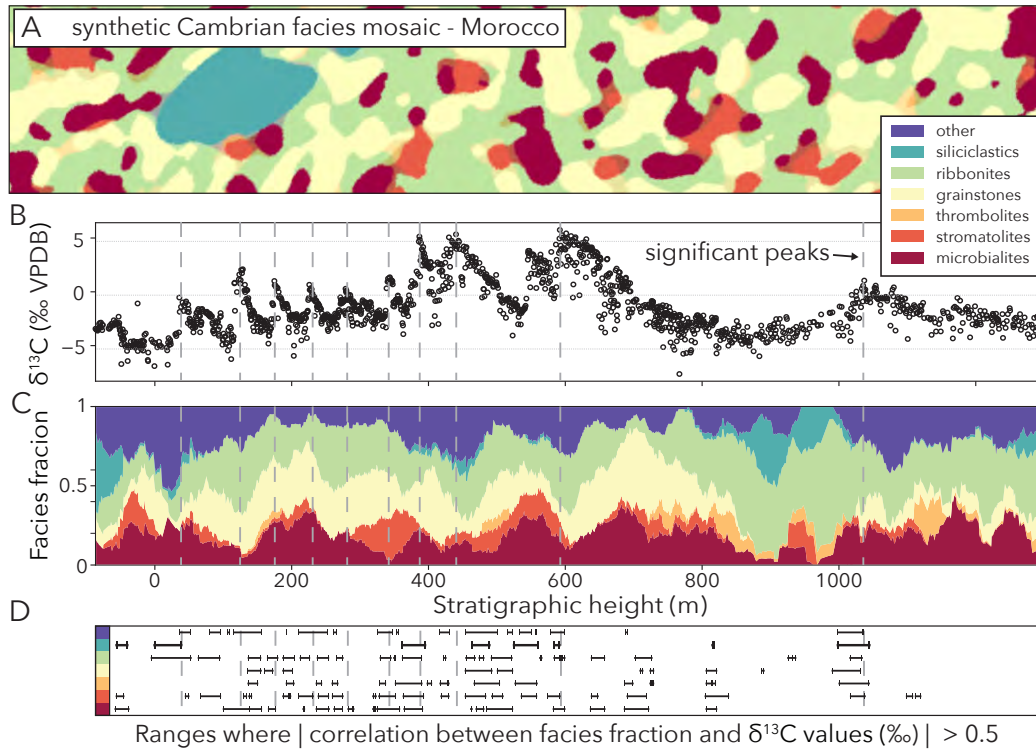
48 Dissimilar to weather and climate data, carbonate stratigraphies also are
49 subject to diagenesis, which occurs after the depositional recording of signals.
50 Once a rock starts to form from sediments, it will be exposed to varying
51 degrees of alteration from factors like early stage fluid flow (Higgins et al.,
52 2018, Ahm et al., 2018) or the influence of basinal fluids at great depths
53 (Swart, 2015, Derry, 2010). Similar to depositional facies, variable exposure
54 of rocks to these alteration factors also can create signals of relatively high
55 magnitude compared to any expected secular change. Even just early stage
56 flow of meteoric waters through Bahamian carbonates drives an additional
57 $\sim 5\%$ variability such that just the last 20 thousand years of stratigraphy on
58 the GBB can replicate the scale of change seen in $\delta^{13}\text{C}$ values over the last
59 two billion years (Geyman and Maloof, 2021).

60 Although recent attention mostly has been given to the impacts of post-
61 burial diagenesis on chemical measurements in carbonates, these processes
62 also are well known to alter fossil occurrences and physical sedimentological
63 data. For an organism's remains to survive burial and exhumation and even-
64 tually be tabulated by a paleontologist, its taphonomic window must align
65 with the diagenetic forces at play to leave a recognizable portion preserved
66 in a way that can be identified (Behrensmeyer et al., 2000, Kidwell et al.,
67 2005). For example, trilobite species counts are impacted both by needing to
68 be buried in an environment that does not dissolve or crush calcitic exoskele-
69 tons, and within a facies that can be split open to view enough diagnostic
70 features for identification (Hughes, 1995). By the same token, the carbonate
71 grains that are observed by a geologist to estimate size distribution or phase

72 modalities can be altered by burial processes that may preferentially destroy
73 or distort certain grain sizes, porosities, and/or mineralogies (Coogan and
74 Manus, 1975).

75 **Correlations between qualitative lithofacies and $\delta^{13}\text{C}$ values in an** 76 **extended lower Cambrian record**

77 Even with shortcomings, qualitative lithologies motivate deeper investi-
78 gation of the influence of depositional environments on carbonate signals. As
79 an example, we perform an exercise on the Moroccan Sidi Msal section and
80 its record of $\delta^{13}\text{C}$ values from Maloof et al. (2010b, Supplementary Figure
81 2), which often are used as a backbone to correlate global early Cambrian
82 timescales and interpret broader changes in the carbon cycle and ocean oxy-
83 genation state (Dahl et al., 2019, Maloof et al., 2010a, Betts et al., 2018,
84 Hay et al., 2019, Smith et al., 2016). Given the relative proportions of cat-
85 egorical facies in the Moroccan sections (Maloof et al., 2010b,a, 2006), we
86 can picture this ancient platform with migrating facies bodies as potential
87 sources of sub-environmental variability (Supplementary Figure 2A). As a
88 first pass in understanding the influence of depositional conditions without *a*
89 *priori* knowledge of $\delta^{13}\text{C}$ distributions on the fossil platform, we look at the
90 relative proportions of qualitative facies categories throughout the section,
91 compared to the isotope curve. We find that the majority of noted peaks and
92 nadirs in the record of $\delta^{13}\text{C}$ values are matched by a peak in prevalence of at
93 least one lithology (Supplementary Figure 2C). The high degree of correla-
94 tion between local facies descriptions and $\delta^{13}\text{C}$ values (Supplementary Figure
95 2D) in a central outcrop for interpreting Cambrian global change, points to
96 the need to develop fine-scale quantitative lithofacies methods to help dis-



Supplementary Figure 2: An exercise investigating the relationship between lithology and $\delta^{13}\text{C}$ values in the Moroccan Sidi Msal section from [Malooof et al. \(2010b\)](#). (A) The proportion of qualitative facies groups reported in these sections ([Malooof et al., 2006, 2010b](#)), create a schematic of what the facies mosaic and sources of spatial variability may have looked like on the ancient platform. (B) The Sidi Msal record of $\delta^{13}\text{C}$ values from [Malooof et al. \(2010b\)](#) provides an expanded record of $\delta^{13}\text{C}$ that covers much of the lower Cambrian. (C) After compiling proportions of the major categorical lithologies in a moving 50 meter window, we find that key features of the record of $\delta^{13}\text{C}$ values are reflected in peaks or nadirs of one or more facies groups. For instance, six of the ten major peaks in $\delta^{13}\text{C}$ values are matched with local maxima in the occurrences of microbialites. (D) This visual correspondence also is reflected in statistical correlations between the facies proportions and $\delta^{13}\text{C}$ values in 50 meter moving windows, where ten of eleven peaks occur during intervals with high Pearson coefficients for at least two facies groups.

97 entangle these relationships. We need to be able to approach questions like:
98 What proportion of peaks and nadirs in the record of $\delta^{13}\text{C}$ values are fully
99 explained by the migration of variable facies and are thus diachronous locally,
100 and not related globally? Of the early Cambrian excursions in $\delta^{13}\text{C}$ values
101 that remain as global and synchronous, are any caused by broad, coordinated
102 shifts in facies that could be expected by an event like sea level rise and are
103 not related to carbon cycling? The remainder of this study aims to introduce
104 means by which we may start to answer such questions.

105 **Stewart's Mill geochronology**

106 Based upon trilobite biostratigraphy, the Stewart's Mill locality falls
107 within the Montezuman Stage of the Waucoban Series (Laurentian equiv-
108 alent of the global Series 2; [Hollingsworth, 2011](#)). The Montezuman stage
109 has no absolute radiometric age constraints, but current estimates from
110 detrital zircon studies, sedimentation rate modeling, and species duration
111 estimates give a maximum span of 5 million years from approximately 519
112 to 514 million years ago ([Peng et al., 2020](#), [Karlstrom et al., 2018](#), [Sund-
113 berg et al., 2020](#)). The lower member of the Poleta Fm is stratigraphically
114 thin compared to the siliciclastic Campito Fm (also within the Montezuman;
115 [Hollingsworth, 2011](#)), and so the carbonates at Stewart's Mill likely only rep-
116 resent a small portion of the possible 5 million year duration. Estimates of
117 time scale for accumulation of the stratigraphy we study at Stewart's Mill
118 are highly uncertain, but these strata may represent 1 million years or less.

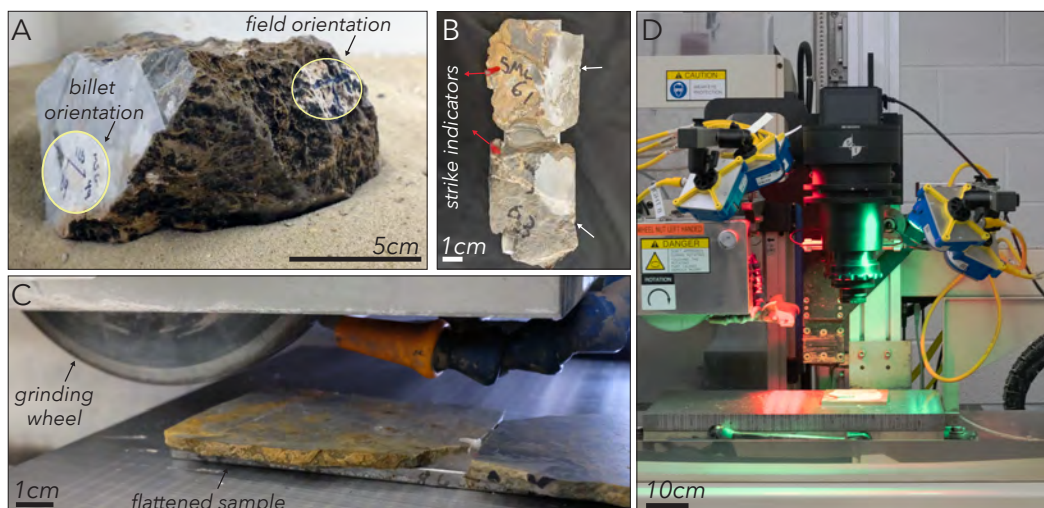
119 Polished slab preparation and imaging

120 *Sample preparation*

121 In preparing polished slabs for imaging, we track cut face orientation in
122 reference to faces marked in the field such that relative orientation of each
123 image, with respect to stratigraphic up and local bedding planes, can be
124 accounted for when assigning metrics. We start by cutting a billet that is
125 large enough to fill the entire $\sim 4.4 \times 5.5$ cm camera field of view (FOV), or
126 as large as possible given the sample size. Following cutting the billet, we
127 loosely place all cut pieces back together and put the entire sample in a sand
128 box to orient it back to field position as indicated by the strike-dip mark and
129 measurement made in the field. Keeping the billet in this position, we then
130 expose the cut face to measure and mark its strike and dip (Supplementary
131 Figure 3A).

132 This cut face of the billet with known orientation will be affixed face-
133 down for grinding, and so the line of strike will not be visible. To track this
134 line, we make a saw mark along the edge of the billet at the front and back
135 of the strike arrow and paint in these saw marks with red to mark the front
136 and white to mark the back (Supplementary Figure 3B). With orientation
137 adequately marked, we affix each billet to a steel plate with 2 ton epoxy and
138 allow 48 hours or longer to cure. The steel plate both acts to increase the
139 robustness of final polished slabs as an archive and allows us to secure slabs
140 to a magnetic chuck for surface grinding.

141 We grind the affixed billets with a Mitsui MSF-818PC-NC CNC surface
142 grinder equipped with a 320 grit diamond wheel, which is the same grinding
143 setup used for 3D modeling with the Grinding Imaging, and Reconstruction



Supplementary Figure 3: Grinding and imaging methods. (A) We place cut billets in a sandbox, rotate into their outcrop orientation based upon strike-dip marked in the field, and mark the orientation of the billet's cut face. (B) Prior to grinding, we mark the ends of the strike-dip arrow on the cut face with paint so the orientation will be constrained even after the cut face is affixed to a steel bar with epoxy. (C) We use a CNC surface grinder to grind all samples flat and parallel. (D). Once samples are polished by hand, we image each rock with a 150 MP achromatic sensor under eight separate narrow-band LEDs to create a multi-spectral image.

144 Instrument (GIRI; Mehra et al., 2022). We grind each sample until enough
 145 parallel, flat area is exposed to fill the camera FOV, aiming to keep a uniform
 146 thickness across the entire sample set (Supplementary Figure 3C). Following
 147 grinding, the samples show some scratch marks from the diamond grit, and
 148 so we polish each slab by hand on a bench top for approximately one minute
 149 each with 600 and 800 grit sandpaper. Although hand polishing greatly
 150 improves the finish on each slab, we prepare each sample for imaging by
 151 applying a thin coat of mineral oil with a foam brush to reduce the specular
 152 appearance of any remaining scratches.

153 *Sample imaging*

154 We image samples with the GIRI camera and reflected light setup de-
155 scribed in [Manzuk et al. \(2022\)](#), equipped with eight narrowband LEDs of
156 the following wavelengths (Supplementary Figure 3D); 365 nm (UV fluores-
157 cence), 470 nm (blue), 505 nm (cyan), 530 nm (green), 590 nm (yellow),
158 625 nm (red), 760 nm (red edge), 940 nm (NIR). Our goal when imaging
159 is to achieve well-exposed images across all samples and wavelengths with-
160 out having to vary shutter speeds between samples. We keep exposure time
161 constant such that we can directly compare pixel intensities from each wave-
162 length between samples as a faithful measure of sample spectral character-
163 istics without having to correct for relative exposure time. To achieve this
164 goal while capturing quality images, we select a subset of six samples that
165 generally span the qualitative lithologic variability in the set to test exposure
166 times. We image each of the test samples with each wavelength at a range
167 of exposure times. For each wavelength, we select the exposure time that
168 gives the largest average spread of pixel values over the test set without any
169 sample images appearing over or under exposed.

170 When imaging the full sample set, we use an ISO of 400 and an f-stop
171 of 8. Our optimized shutter speeds for this sample set are; 365 nm - 8s,
172 470 nm - 0.6s, 505 nm - 0.5s, 530 nm - 0.5s, 590 nm - 0.8s, 625 nm $\frac{1}{3}$ s,
173 760 nm - 0.5s, 940 nm - 0.6s. The room is kept completely dark throughout
174 imaging such that the only light in photographs comes from the reflection
175 of the narrowband LEDs. The camera is attached directly to the surface
176 grinder, and so we place samples on the magnetic chuck for imaging and
177 use the grinder controls to move samples into the FOV. Because we know all

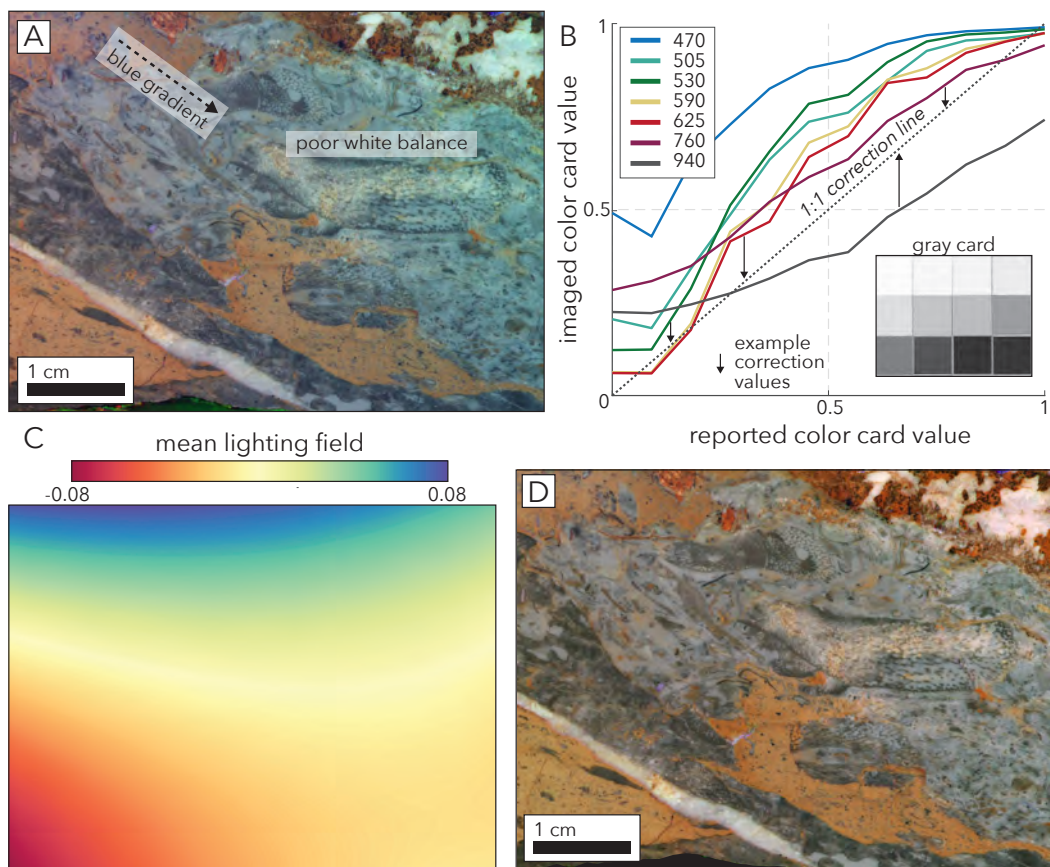
178 samples are ground parallel with respect to the chuck with constant thickness,
179 we ensure that all images are well focused, even with the narrow depth of
180 field for the camera. An automated program written in Matlab interfaces
181 with the camera and lights to take all images automatically in sequence.

182 We image all samples with a Phase One IQ4 150-megapixel digital back
183 with sensor dimensions of 4.04×5.37 cm. We use a 120 mm Schneider
184 Kreuznach apochromatic macro lens, which gives a field of view and pixel
185 resolution equal to the dimensions of the digital back. The final spatial
186 resolution in these images is $3.76 \mu\text{m}$ per pixel.

187 As mentioned in [Manzuk et al. \(2022\)](#), these sample images suffer from
188 some chromatic aberration, whereby each wavelength achieves maximal sharp-
189 ness at a different focal depth due to the wavelength dependence of light
190 refraction. In our imaging protocol, we keep 530 nm (green) as the maxi-
191 mally sharp wavelength, and model the blur in all subsequent wavelengths
192 using the protocols of [Manzuk et al. \(2022\)](#). Deconvolving to sharpen im-
193 ages is computationally expensive, and so we only apply this operation when
194 sharpness in a separate wavelength is expressly necessary.

195 *Sample spectral signature*

196 The first basic property of a rock sample that is useful for distinction
197 and categorization is color—both what we can see with our eyes, as well as
198 additional spectral characteristics of minerals that are invisible to humans.
199 For example, in our samples the amount of microbialite is indicated by dark
200 blue hues, and overall UV fluorescence tracks the degree of recrystallization.
201 Our standardized imaging protocols across all samples already assure we



Supplementary Figure 4: Protocols for white balance and correcting lighting unevenness to assure accurate assessment of relative color over samples. (A) An example red-green-blue composite assembled from the raw images shows both the poor white balance and color gradients that result from imaging conditions. (B) The difference between the reported value for each gray level, and the actual value recorded by the camera sensor serves as a correction factor tailored across all wavelengths. (C) An example surface fit to the mean lighting field for 470 nm (blue) shows the unevenness in intensity with a general gradient that runs away from the light source, which was situated to the upper left of all samples. This surface serves as a pixel-wise correction factor with which we subtract to correct for the exact nature of lighting unevenness for each wavelength. (D) After white balancing and correcting for lighting unevenness, we achieve realistic composite images that are ready for color comparison and other quantitative analyses.

202 have comparable color signals, but we perform some corrections to make
203 our images a petrographic record that is faithful to the geologist's eye and
204 removes some imperfections.

205 Because our imaging protocols do not keep exposure times constant across
206 all wavelengths, and the intensity of light from each LED that reaches the
207 sample may vary, the colors in our raw images are not balanced. So, a gray
208 patch of a sample, which should have an even reading for each wavelength,
209 instead appears as whichever color has the highest combination of light in-
210 tensity and exposure time (often blue in our images; Supplementary Figure
211 4A). To achieve white/gray balanced images, we image a matte ColorGauge
212 Micro target under the same lighting and exposure settings used for samples,
213 specifically looking at the twelve squares that show black, various grays, and
214 white. We get the mean color values for each square, over each wavelength,
215 and interpolate to get a curve through these gray levels (Supplementary Fig-
216 ure 4B). The difference between our experimental curves, and interpolated
217 reported gray values from the target, serve as correction factors that redis-
218 tribute pixel values to be balanced across wavelengths and produce more
219 realistic composite images (Supplementary Figure 4D). We keep these cor-
220 rections constant across samples to maintain color as a meaningful metric
221 for comparing lithofacies.

222 This sample set was imaged with only a single LED for each wavelength
223 and so the raking light is of slightly uneven intensity across the camera FOV
224 (the narrowband light source for the imaging setup has since been changed
225 to a ring light to improve evenness and reduce specularly). To correct this
226 pattern and assure that all parts of the sample image have equal expression

227 of relative brightness, we assess the mean lighting field for all wavelengths to
228 be the mean of all sample images (Supplementary Figure 4C). Because some
229 samples do not fit the full field of view, the edges of the mean image are less
230 reliable, so we fit a surface to the center of the mean image to extrapolate
231 to the edges. This surface then gives a correction value to add or subtract
232 to each pixel based upon its location in the image. Once corrected, we
233 successfully remove any color gradients on samples that result from uneven
234 lighting (Supplementary Figure 4D).

235 Following our imaging protocols and color corrections, we have multi-
236 spectral images that are a faithful record of sample color to be input to
237 quantitative lithofacies comparison.

238 **Geochemical measurements**

239 *Measurement of $\delta^{13}\text{C}$ and $\delta^{18}\text{O}$ values*

240 We place approximately 0.25 mg (measured volumetrically via a labora-
241 tory standard) of sample powders in individual borosilicate reaction vessels,
242 heat to 110 °C to remove volatiles, and cap the vessels. We then flush the
243 vials with He to remove atmospheric gas and react the powders with five
244 drops of H_3PO_4 . We measure the CO_2 analyte with a Sercon IRMS coupled
245 with a GasBench II sampling device. To monitor precision and accuracy of
246 our measurements of $\delta^{13}\text{C}$ and $\delta^{18}\text{O}$ values, we analyze 15 standards (IAEA-
247 603, $n = 4$, as well as two laboratory standards, $n = 2$ and 9 respectively,
248 with known $\delta^{13}\text{C}$ and $\delta^{18}\text{O}$ values) for every 57 samples.

249 To reduce data and report final $\delta^{13}\text{C}$ and $\delta^{18}\text{O}$ values with uncertainties,
250 we regress the δ value versus area for seven peaks per sample and standard.
251 This regression, sometimes referred to as a linearity or peak size correction,

252 corrects for differences in sampling peak intensity arising from volumet-
253 ric measurement or mineralogical differences between analytes (Dunn and
254 Carter, 2018). We report $\delta^{13}\text{C}$ and $\delta^{18}\text{O}$ values in standard delta notation
255 relative to the Vienna Pee Dee Belemnite (V-PDB). To convert to V-PDB
256 values, we use the average conversion given by IAEA-603 ($\delta^{13}\text{C} = 2.46\text{‰} \pm$
257 0.01 , $\delta^{18}\text{O} = -2.37\text{‰} \pm 0.25$) and our internal VTS standard ($\delta^{13}\text{C} = -1.48\text{‰}$
258 ± 0.07 , $\delta^{18}\text{O} = -8.54\text{‰} \pm 0.14$). The values we report for mean value and
259 precision of the VTS standard come from internal long-term laboratory av-
260 erages and standard deviations ($n = 2,550$). Our laboratory reproduces the
261 reported values for IAEA-603 on the long term long-term with a precision of
262 <0.09 for $\delta^{13}\text{C}$ and <0.16 for $\delta^{18}\text{O}$ (1σ , $n = 145$).

263 Our laboratory tolerances in terms of standard deviation of δ value over a
264 single run in order to use a standard for conversion are $\pm 0.1\text{‰}$ for $\delta^{13}\text{C}$ values
265 and $\pm 0.25\text{‰}$ for $\delta^{18}\text{O}$ values. In 3/19 machine runs, the IAEA standard
266 was found to give values outside of laboratory tolerances. In such cases, we
267 use a single point correction with VTS as the more reproducible standard
268 for that run. We measure single replicates for each sample. In cases where
269 the standard deviation for a sample's seven peak measurements (following
270 correction for peak area via regression) exceeds our laboratory tolerances,
271 we measure a duplicate and only report values for samples that achieve our
272 precision tolerances.

273 *Minor and trace element measurements*

274 These measurements are made on the same sampled powders as the mea-
275 surements of stable isotope ratios. For each sample, we react 1–5 mg of car-
276 bonate powder with a 0.25M buffered acetic acid solution ($\text{pH} \sim 5$; Reagents

277 are TraceMetal Grade Ammonium Hydroxide, and TraceMetal Grade Acetic
278 Acid, Glacial from Fisher Chemical - Fisher Scientific Company, LLC.) in a
279 15 mL Falcon tube, using approximately 1 mL of solution per 1 mg of powder.
280 Prior to use, we acid wash the Falcon tubes in 2% HNO₃, rinse thoroughly
281 with 18.2 MΩ·cm Milli-Q water, and allow to dry. We leave the sample-acid
282 mixtures to digest for four hours in a sonicator, and then centrifuge the tubes
283 for 30 minutes at 2500 rpm. We then transfer the supernatant liquid to a
284 second acid-washed Falcon tube for analysis. This digestion method readily
285 dissolves carbonates but leaves insoluble material, like clays and metal ox-
286 ides, thereby minimizing ion extraction from co-occurring silicate minerals
287 ([Tessier et al., 1979](#)).

288 We measure minor and trace element concentrations with Thermo Fisher
289 I-Cap Q inductively coupled plasma mass spectrometer (ICP-MS). To quan-
290 tify elements spanning a wide range of concentrations, we analyze each sam-
291 ple at two dilution levels prepared in 2% ultra-trace HNO₃. We prepare
292 a low-concentration aliquot at 50-fold dilution and a higher-concentration
293 aliquot at 17-fold dilution. The less-dilute (17-fold) solutions yielded repro-
294 ducible measurements for Mg, Ca, Mn, and Fe, whereas Sr concentrations
295 in some samples exceeded the calibration range at this dilution level. The
296 higher dilution (50-fold) solutions consistently yielded reproducible quanti-
297 fications of Mg, Ca, and Sr. We report all elemental concentrations as molar
298 ratios normalized to Ca. For each reported elemental ratio, values reflect the
299 mean of two replicate measurements (n=2) when both dilution levels yielded
300 results within the calibration range.

301 We base quantifications on four multi-element carbonate matrix-matched

302 calibration standards. We prepare additional dilutions of these standards to
303 produce a 10-point calibration curve spanning the concentration range of the
304 analyzed samples. We run all 10 calibration standards at the beginning and
305 end of each analytical sequence, with approximately 70 unknown samples
306 analyzed per run. We only retain samples with signal intensities within the
307 calibration range. For a run, we require calibration curves to have an R^2
308 value > 0.99 for the reported analyte. We rerun samples and standards
309 when this criterion is not met.

310 We internally spike all samples, standards, and blanks with ~ 500 ppb
311 ^{115}In to monitor and correct for short-term instrumental drift during analysis.
312 Each analytical run also includes four procedural blank solutions consisting
313 of the same 2% ultra-trace HNO_3 used for sample dilution. We use these
314 blanks for blank subtraction during data reduction.

315 We monitor analytical reproducibility and accuracy by repeated analysis
316 of the NIST SRM 88b standard, included 2-4 times during each analytical
317 run. Long-term measurements of the standard have a precision better than
318 $\pm 5\%$ (1σ , $n=120$) for all reported elemental ratios. Our laboratory value for
319 NIST SRM 88b is within uncertainty of accepted ratio values.

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